

MATH 3334 Advanced Multivariable and Vector Calculus

1. *Course number and name:* MATH 3334 – Advanced Multivariable and Vector Calculus
2. *Credits and contact hours:* 3 Semester Credit Hours (3 SCH) – 3 contact hours per week
3. *Instructor's or course coordinator's name:* Gabriela Jaramillo, Assistant Professor of Mathematics
4. *Text book, title, author, and year:*
 - a. “Advanced Calculus” by James J. Callahan, 2010.
 - b. “Vector Calculus, Linear Algebra, and Differential Forms”, by John H. Hubbard and Barbara Burke Hubbard, 2015.
 - c. “Introduction to Vector Analysis”, by Harry F. Davis and A. David Snider, 2016.
5. *Specific course information*
 - a. *brief description of the content of the course (catalog description):* Basic theory underlying multivariable and vector calculus, with applications. Topics include topology of n -space, derivative of a multivariable function as a linear transformation and applications, multivariable Taylor theorem, the inverse and implicit function theorems; calculus of vector fields and vector differential operators, Stokes and Gauss integral theorems, physical applications.
 - b. *prerequisites or co-requisites:* MATH 2318 and MATH 3333, or MATH2318 and currently enrolled in MATH 333 with approval of instructor.
 - c. *indicate whether a required, elective, or selected elective (as per Table 5-1) course in the program:* N/A.
6. *Specific goals for the course*
 - a. *specific outcomes of instruction, ex. The student will be able to explain the significance of current research about a particular topic:* Upon completion of this course, the students are expected to gain an understanding of the topology of \mathbb{R}^n ; multivariable differentiation; Taylor's theorem in several variables; implicit and inverse function theorems; algebra of vectors and vector differential operators; line, surface and volume integrals, including Green's, Stokes' and Divergence theorems, and curvilinear coordinates.
 - b. *explicitly indicate which of the student outcomes listed in Criterion 3 or any other outcomes are addressed by the course:* This course addresses Student Outcome a.

7. *Brief list of topics to be covered:*

- Topology of \mathbb{R}^n : open closed sets, limits of functions and continuity, the Extreme Value Theorem on \mathbb{R}^n .
- Multivariable Differentiation: the derivative of a function as a linear map and implications. Taylor's Theorem in several variables, Implicit and Inverse Function Theorems.
- Multivariable Integration: double and triple integrals, Fubini's Theorem, change of variables formula.
- Scalar and Vector Fields: Scalar fields and gradients. Introduction to vectors; scalar and vector products. Vector fields and grad, div, curl, and Del notation in rectangular, cylindrical and spherical coordinates.
- Line, surface and volume integrals, characterization of irrotational fields.
- Green's Theorem, The Divergence Theorem and Stokes' Theorem in 3 dimensions and associated theorems. Applications.